| $\Delta \beta$ | average error in solute distribution ra | tio |
|----------------|---|-----|
|                | 11 11 <b>661</b> 1 11                   |     |

 $\gamma$ activity coefficient

## Subscripts

| I, J | components i and j           |
|------|------------------------------|
| j    | phase /, eq 1 and 2          |
| k    | tie line <i>k</i>            |
| n    | 1, 2,, NP (parameters, eq 1) |
| S    | solute                       |
| œ    | infinite dilution            |

## Superscripts

|    | calculated values        |
|----|--------------------------|
| τ. | <br>the set Trend TTrend |

I. II phases I and II, eq 1

Registry No. Acetic acid, 64-19-7; methyl isopropyl ketone, 563-80-4.

# Literature Cited

- (1) Renon, H.; Prausnitz, J. M. AIChE J. 1968, 14, 135-144.
- Abrams, D. S.; Prausnitz, J. M. AIChE J. 1975, 21, 116–128.
   Fredenslund, Aa.; Jones, R. L.; Prausnitz, J. M. AIChE J. 1975, 21,
- 1086-1099. (4) Magnussen, T.; Rasmussen, P.; Fredenslund, Aa. Ind. Eng. Chem.
- Process Des. Dev. 1981, 20, 331-339. (5) Othmer, D. F.; White, R. E.; Trueger, E. Ind. Eng. Chem. 1941, 33,
- 1240-1248.
- Correa, J. M. Determinación, correlación y predicción del equilibrio líquido-líquido. Sistemas Agua + Acido acético + Cetonas. Doctoral Thesis, Universidad de Santlago de Compostela, Spain, 1985 (7) Gross, P. M.; Rintelen, J. C.; Saylor, J. M. J. Phys. Chem. 1939, 43,
- 197-205. (8) Ginnings, P. M.; Pionk, D.; Carter, E. J. Am. Chem. Soc. 1940, 62,
- 1923-1924. (9) Sørensen, J. M. Correlation of liquid-liquid equilibrium data. Ph.D. The-
- sis, Technical University of Denmark, Lyngby, Denmark, 1980. (10) Correa, J. M.; Arce, A.; Blanco, A.; Correa, A. Fluid Phase Equilib. 1987, 32, 151-162.

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# High-Pressure Vapor-Liquid Equilibria of Mixtures of Nitrogen, **Carbon Dioxide, and Cyclohexane**

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Data are reported for the equilibrium phase compositions and densities of the carbon dioxide + cyclohexane and the nitrogen + cyclohexane systems at 366.5 and 410.9 K and for the nitrogen + carbon dioxide + cyclohexane system at the same temperatures at a variety of isobars. These data were modeled with the Peng-Robinson equation of state with generalized parameters. Good fits were obtained for the compositions in all three systems, but the predicted liquid-phase densities were in error by about 5%, as expected.

# Introduction

The motivation for this research is to obtain experimental data on systems consisting of hydrocarbons and carbon dioxide, nitrogen, and other non-hydrocarbons, and to utilize these data in evaluating equations of state and their mixing rules. By determining both the compositions and the densities of the coexisting phases, equations of states and their mixing rules can be more stringently tested than with composition data alone.

The equipment used in these measurements is the doublerecirculation cell with a maximum temperature of 300 °F and maximum pressure of 5000 psla described earlier (1). The key components of the apparatus are a 100-cm<sup>3</sup> through-windowed visual cell, recirculation pumps, and vibrating-tube density meters. The operating procedure for this equipment has also been described earlier (1) and will not be repeated here.

## **Experimental Results**

Table I contains our unsmoothed, experimental data for the CO<sub>2</sub> + cyclohexane system at 366.5 and 410.9 K. Data for this system, at different temperatures, have been reported Table I. Vapor-Liquid Equilibrium Data for the Carbon Dioxide + Cyclohexane Binary System

| <i>Т</i> , К | P, bar | $x_{\rm CO_2}$ | $y_{\rm CO_2}$ | $ ho_{ m L}$ , g/cm <sup>3</sup> | $ ho_{ m V},{ m g/cm^3}$ |
|--------------|--------|----------------|----------------|----------------------------------|--------------------------|
| 366.5        | 1.71   | 0.0000         | 0.0000         | 0.7050                           | 0.0077                   |
| 366.4        | 17.52  | 0.0959         | 0.8984         | 0.7059                           | 0.0288                   |
| 366.4        | 34.69  | 0.1681         | 0.9374         | 0.7071                           | 0.0593                   |
| 366.5        | 51.91  | 0.2657         | 0.9495         | 0.7074                           | 0.0940                   |
| 366.5        | 68.86  | 0.3484         | 0.9515         | 0.7060                           | 0.1349                   |
| 366.6        | 86.37  | 0.4598         | 0.9500         | 0.7019                           | 0.1831                   |
| 366.5        | 103.60 | 0.5698         | 0.9402         | 0.6894                           | 0.2476                   |
| 366.5        | 125.11 | 0.7526         | 0.8977         | 0.6222                           | 0.3986                   |
| 366.4        | 128.00 | 0.7901         | 0.8732         | 0.5807                           | 0.4515                   |
| 410.8        | 4.43   | 0.0000         | 0.0000         | 0.6566                           | 0.0114                   |
| 410.8        | 17.18  | 0.0671         | 0.7166         | 0.6584                           | 0.0294                   |
| 410.9        | 34.44  | 0.1470         | 0.8295         | 0.6544                           | 0.0570                   |
| 410.9        | 51.51  | 0.2050         | 0.8593         | 0.6553                           | 0.0866                   |
| 410.8        | 69.28  | 0.2887         | 0.8850         | 0.6488                           | 0.1198                   |
| 410.9        | 86.51  | 0.3578         | 0.8861         | 0.6434                           | 0.1614                   |
| 410.9        | 104.02 | 0.4329         | 0.8777         | 0.6312                           | 0.2046                   |
| 410.9        | 120.56 | 0.5165         | 0.8636         | 0.6151                           | 0.2579                   |
| 410.9        | 138.14 | 0.6107         | 0.8320         | 0.5733                           | 0.3434                   |
| 410.8        | 144.41 | 0.6850         | 0.7846         | 0.5232                           | 0.4115                   |
| 410.9        | 145.10 | 0.7448         | 0.7671         | 0.4893                           | 0.4321                   |

previously by Krichevskii and Sorina (2). Figures 1 and 2 are plots of composition and density for both data sets. Since the temperatures of the data sets are different, the data cannot be directly compared.

The data for the  $N_2$  + cyclohexane system are tabulated in Table II. Two isotherms, 366.5 and 410.9 K, were measured for this system. The previously measured bubble-point data of Khodeeva (3) are plotted and compared with our experimental data in Figure 3, though the temperatures are not quite the same. Our density data are shown in Figure 4; there are no published density data for this system.

Tables III and IV contain our experimental, unsmoothed data for the  $N_2 + CO_2 + cyclohexane$  system at 366.5 and 410.9 K with data taken at four pressures, 68.9, 137.9, 206.8, and 275.7 bar, at both temperatures. No data for this system have been reported previously. Figures 5-8 are composition and density plots of these data sets.

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Figure 1. T-P-x-y data for carbon dioxide + cyclohexane. A comparison of experimental data from this study with that of Krichevskii and Sorina (2) at somewhat different temperatures. The data have been fit with the Peng-Robinson equation of state (solid lines).

Table II. Vapor-Liquid Equilibrium Data for the Nitrogen + Cyclohexane Binary System

| <i>T</i> , K | P, bar | $x_{N_2}$ | $y_{N_2}$ | $ ho_{ m L}$ , g/cm <sup>3</sup> | $\rho_{\rm V},{\rm g/cm^3}$ |
|--------------|--------|-----------|-----------|----------------------------------|-----------------------------|
| 366.5        | 1.71   | 0.0000    | 0.0000    | 0.7050                           | 0.0077                      |
| 366.5        | 17.99  | 0.0094    | 0.9064    | 0.7034                           | 0.0194                      |
| 366.5        | 34.85  | 0.0337    | 0.9422    | 0.7032                           | 0.0358                      |
| 366.4        | 69.83  | 0.0678    | 0.9673    | 0.7031                           | 0.0685                      |
| 366.4        | 103.88 | 0.0985    | 0.9713    | 0.7024                           | 0.1004                      |
| 366.4        | 138.76 | 0.1286    | 0.9721    | 0.7017                           | 0.1324                      |
| 366.4        | 172.53 | 0.1571    | 0.9719    | 0.7017                           | 0.1626                      |
| 366.5        | 207.00 | 0.1802    | 0.9676    | 0.7015                           | 0.1929                      |
| 366.3        | 241.94 | 0.2088    | 0.9694    | 0.7011                           | 0.2204                      |
| 366.6        | 275.93 | 0.2438    | 0.9664    | 0.7015                           | 0.2485                      |
| 410.8        | 4.43   | 0.0000    | 0.0000    | 0.6566                           | 0.0114                      |
| 410.8        | 17.53  | 0.0169    | 0.7133    | 0.6606                           | 0.0226                      |
| 410.9        | 35.27  | 0.0343    | 0.8381    | 0.6612                           | 0.0388                      |
| 410.9        | 69.14  | 0.0721    | 0.9124    | 0.6606                           | 0.0689                      |
| 410.8        | 103.74 | 0.1116    | 0.9154    | 0.6594                           | 0.0997                      |
| 410.8        | 138.21 | 0.1478    | 0.9230    | 0.6574                           | 0.1297                      |
| 410.9        | 172.74 | 0.1821    | 0.9224    | 0.6542                           | 0.1593                      |
| 410.8        | 206.86 | 0.2161    | 0.9202    | 0.6522                           | 0.1877                      |
| 410.8        | 241.46 | 0.2552    | 0.9198    | 0.6494                           | 0.2163                      |
| 410.9        | 275.79 | 0.2906    | 0.9121    | 0.6473                           | 0.2449                      |

The data for the  $CO_2$  + cyclohexane and  $N_2$  + cyclohexane binary systems have been correlated with the Peng-Robinson equation of state (4) and the van der Waals one-fluid mixing rules

$$P = \frac{RT}{V - b} - \frac{a}{V(V + b) + b(V - b)}$$
(1)

$$a = \sum_{i=1}^{n_{o}} \sum_{j=1}^{n_{o}} x_{i} x_{j} a_{ij}$$
(2)

$$b = \sum_{i=1}^{n_c} x p_i \tag{3}$$

$$b = \sum_{i=1}^{n} \lambda p_i \qquad (0)$$

$$a_{ij} = (a_{ij}a_{jj})^{0.5}(1 - k_{ij})$$
(4)

The fits of the  $CO_2$  + cyclohexane compositional data with the Peng-Robinson EOS and van der Waals one fluid mixing rules are shown as the solid lines in Figures 1 and 2. One



Figure 2. Phase density data for carbon dioxide + cyclohexane. A comparison of experimental data from this study with that of Krichevskii and Sorina (2) at somewhat different temperatures. The solid lines result from the Peng-Robinson equation of state with the binary parameter determined from fitting compositional data.



Figure 3. T-P-x-y data for nitrogen + cyclohexane. A comparison of experimental data from this study with that of Khodeeva (3) at somewhat different temperatures. The data have been fit with the Peng-Robinson equation of state and a single binary parameter.

adjustable interaction parameter  $k_{ij}$  fitted to the T-P-x-y data is adequate for modeling the compositional data for this system, though the critical pressure is overpredicted. An isothermal flash routine was used in the fitting of the binary interaction parameter, since we feel the error in our vapor and liquid compositions to be equal, at about 0.005 mole fraction. The objective function used in the fitting was

OBJ = 
$$\sum_{j=1}^{\text{NPTS}} \sum_{n=1}^{n_c} (|x_j^{\text{CALC}} - x_j^{\text{EXP}}| + |y_j^{\text{CALC}} - y_j^{\text{EXP}}|)$$
 (5)

and



Figure 4. Phase density data for the nitrogen + cyclohexane system. The solid lines are the predictions of the Peng-Robinson equation of state with the single binary parameter fit to compositional data.



Journal of Chemical and Engineering Data, Vol. 34, No. 4, 1989 421



Figure 6. Phase behavior for the ternary system of nitrogen, carbon dioxide, and cyclohexane at T = 410.9 K and four pressures. The solid lines are the Peng-Robinson predictions based on binary data.

dictions of the  $CO_2$  + cyclohexane phase density data using the  $k_{ij}$  determined from fitting the T-P-x-y data are less satisfactory, as is expected. The differences between the experimental and calculated densities are most noticeable in the liquid and near the mixture critical point of each isotherm. Note that the phase densities were not used in fitting the binary interaction parameter, nor would including them have improved the fit significantly.

The fits of the N<sub>2</sub> + cyclohexane data with the Peng-Robinson EOS and van der Waals one-fluid mixing rules are shown in Figures 3 and 4. The fit of the compositional data is generally quite good up to the highest pressure ( $\sim$ 276 bar) which is well below the critical point for this mixture at the temperatures studied. Again the liquid density predictions are in error by as much as 5%. In a subsequent paper we will discuss alternative modeling techniques to improve the density predictions.

The phase behavior of the ternary  $N_2 + CO_2 + cyclohexane$ system was predicted by using the binary parameters determined from our binary data, though setting  $k_{ij}$  for the N<sub>2</sub>-CO<sub>2</sub> system equal to zero as reported elsewhere (1). The accuracy of the composition predictions for ternary mixtures depends on the fit of the binary systems (i.e., the  $N_2$  + cyclohexane, CO<sub>2</sub> + cyclohexane, and  $N_2$  + CO<sub>2</sub> systems). Since the fit of the N<sub>2</sub> + cyclohexane and CO<sub>2</sub> + cyclohexane binary systems with the Peng-Robinson equation of state, the van der Waals onefluid mixing rules, and a single binary interaction parameter was quite good, the quality of the ternary predictions is satisfactory (Figures 5 and 6). However, similar to the fits of the binary data,

Figure 5. Phase behavior for the ternary system of nitrogen, carbon dioxide, and cyclohexane at T = 366.5 K and four pressures.

Optimum fits of the isotherms were determined by allowing the  $k_{\mu}$  parameter to be temperature dependent (Table V). Pre-

| Table III. | Vapor-Liquid Equilbrium Data for the Nitrogen | + Carbon | Dioxide + | Cyclohexane | Ternary | System a | t 366.5 K |
|------------|---|----------|-----------|-------------|---------|----------|-----------|
| (200 °F)   |   |          |           |             |         |          |           |

| <i>T</i> , K | P, bar              | $x_{N_2}$ | $x_{\rm CO_2}$ | $\mathcal{Y}_{N_2}$ | $\mathcal{Y}_{CO_2}$ | $ ho_{ m L}$ , $ m g/cm^3$ | $\rho_{\rm V},{ m cm}^3$ |
|--------------|---------------------|-----------|----------------|---------------------|----------------------|----------------------------|--------------------------|
| 366.4        | 69.83               | 0.0678    | 0.0000         | 0.9673              | 0.0000               | 0.7031                     | 0.0685                   |
| 366.5        | 69.00               | 0.0603    | 0.0284         | 0.8568              | 0.1048               | 0.7041                     | 0.0729                   |
| 366.5        | 69.00               | 0.0533    | 0.0675         | 0.7187              | 0.2386               | 0.7045                     | 0.0792                   |
| 366.5        | 69.00               | 0.0459    | 0.1021         | 0.6007              | 0.3514               | 0.7052                     | 0.0856                   |
| 366.4        | 69.14               | 0.0374    | 0.1621         | 0.4219              | 0.5351               | 0.7057                     | 0.0971                   |
| 366.4        | 69.28               | 0.0303    | 0.2100         | 0.3054              | 0.6562               | 0.7060                     | 0.1055                   |
| 366.5        | 68.86               | 0.0251    | 0.2486         | 0.2057              | 0.7559               | 0.7060                     | 0.1134                   |
| 366.3        | 68.86               | 0.0179    | 0.2894         | 0.1253              | 0.8349               | 0.7057                     | 0.1201                   |
| 366.5        | 68.86               | 0.0000    | 0.3484         | 0.0000              | 0.9515               | 0.7060                     | 0.1349                   |
| 366.4        | 138.76              | 0.1286    | 0.0000         | 0.9721              | 0.0000               | 0.7017                     | 0.1324                   |
| 366.4        | 138.20              | 0.1138    | 0.0776         | 0.7974              | 0.1678               | 0.7031                     | 0.1499                   |
| 366.5        | 137.79              | 0.1041    | 0.1360         | 0.6794              | 0.2788               | 0.7030                     | 0.1644                   |
| 366.5        | 138.07              | 0.0961    | 0.1981         | 0.5710              | 0.3830               | 0.7024                     | 0.1804                   |
| 366.4        | <b>137.9</b> 3      | 0.0862    | 0.2750         | 0.4518              | 0.4975               | 0.7010                     | 0.2019                   |
| 366.4        | <b>137.9</b> 3      | 0.0705    | 0.3697         | 0.3224              | 0.6265               | 0.6970                     | 0.2333                   |
| 366.5        | 138.07              | 0.0539    | 0.5041         | 0.1842              | 0.7572               | 0.6847                     | 0.2877                   |
| 366.5        | 137.79              | 0.0365    | 0.6722         | 0.0705              | 0.8357               | 0.6394                     | 0.3856                   |
| 366.5        | 137.93              | 0.0339    | 0.7358         | 0.0434              | 0.8387               | 0.5952                     | 0.4449                   |
| 366.5        | 207.00              | 0.1802    | 0.0000         | 0.9676              | 0.0000               | 0.7015                     | 0.1929                   |
| 366.5        | 206.86              | 0.1737    | 0.0784         | 0.7911              | 0.1594               | 0.7014                     | 0.2150                   |
| 366.6        | 206.86              | 0.1623    | 0.1481         | 0.7155              | 0.2383               | 0.7001                     | 0.2384                   |
| 366.5        | 206.86              | 0.1591    | 0.3010         | 0.5072              | 0.4289               | 0.6927                     | 0.2956                   |
| 366.6        | 206.58              | 0.1481    | 0.4124         | 0.3752              | 0.5463               | 0.6786                     | 0.3542                   |
| 366.5        | 206.58              | 0.1443    | 0.5287         | 0.2831              | 0.6155               | 0.6478                     | 0.4256                   |
| 366.3        | 207.00              | 0.1564    | 0.5802         | 0.2341              | 0.6320               | 0.6106                     | 0.4821                   |
| 366.6        | 275. <del>9</del> 3 | 0.2438    | 0.0000         | 0.9664              | 0.0000               | 0.7015                     | 0.2485                   |
| 366.5        | 275.65              | 0.2274    | 0.0987         | 0.8140              | 0.1413               | 0.6991                     | 0.2823                   |
| 366.4        | 275.79              | 0.2252    | 0.1736         | 0.7085              | 0.2341               | 0.6955                     | 0.3151                   |
| 366.5        | 275.65              | 0.2229    | 0.2677         | 0.5858              | 0.3378               | 0.6877                     | 0.3577                   |
| 366.5        | 275.79              | 0.2244    | 0.3525         | 0.4861              | 0.4153               | 0.6733                     | 0.4082                   |
| 366.4        | 275.65              | 0.2404    | 0.4287         | 0.3977              | 0.4705               | 0.6447                     | 0.4698                   |
| 366.5        | 275.65              | 0.2711    | 0.4687         | 0.3453              | 0.4862               | 0.6081                     | 0.5202                   |

Table IV. Vapor-Liquid Equilibrium Data for the Nitrogen + Carbon Dioxide + Cyclohexane Ternary System at 410.9 K (280 °F)

| Т, К  | P, bar              | $x_{N_2}$ | x <sub>CO2</sub> | $\mathcal{Y}_{N_2}$ | yco2   | $ ho_{ m L},{ m g/cm^3}$ | $ ho_{ m V},{ m g/cm^3}$ |
|-------|---------------------|-----------|------------------|---------------------|--------|--------------------------|--------------------------|
| 410.9 | 69.14               | 0.0721    | 0.0000           | 0.9124              | 0.0000 | 0.6606                   | 0.0689                   |
| 410.8 | 69.00               | 0.0770    | 0.0144           | 0.8499              | 0.0569 | 0.6591                   | 0.0703                   |
| 410.9 | 68.86               | 0.0670    | 0.0327           | 0.7601              | 0.1385 | 0.6591                   | 0.0743                   |
| 410.8 | 68.86               | 0.0537    | 0.0704           | 0.6087              | 0.2776 | 0.6587                   | 0.0804                   |
| 410.8 | 69.00               | 0.0511    | 0.1017           | 0.4897              | 0.3958 | 0.6581                   | 0.0870                   |
| 410.8 | 68.86               | 0.0423    | 0.1333           | 0.3724              | 0.5194 | 0.6568                   | 0.0932                   |
| 410.8 | 69.00               | 0.0333    | 0.1635           | 0.2722              | 0.6194 | 0.6569                   | 0.0999                   |
| 410.8 | 69.00               | 0.0257    | 0.1930           | 0.1816              | 0.7120 | 0.6565                   | 0.1059                   |
| 410.9 | 69.07               | 0.0150    | 0.2239           | 0.0876              | 0.8009 | 0.6556                   | 0.1132                   |
| 410.8 | 69.28               | 0.0000    | 0.2887           | 0.0000              | 0.8850 | 0.6488                   | 0.1198                   |
| 410.8 | 138.21              | 0.1478    | 0.0000           | 0.9230              | 0.0000 | 0.6574                   | 0.1297                   |
| 410.8 | 138.07              | 0.1308    | 0.0758           | 0.7348              | 0.1796 | 0.6542                   | 0.1471                   |
| 410.8 | 138.07              | 0.1242    | 0.1094           | 0.6577              | 0.2469 | 0.6523                   | 0.1555                   |
| 410.9 | 137.93              | 0.1114    | 0.1704           | 0.5305              | 0.3748 | 0.6504                   | 0.1712                   |
| 410.8 | 137. <del>9</del> 3 | 0.0964    | 0.2161           | 0.4465              | 0.4478 | 0.6468                   | 0.1845                   |
| 410.9 | 137. <b>9</b> 3     | 0.0809    | 0.2889           | 0.3270              | 0.5636 | 0.6415                   | 0.2068                   |
| 410.9 | 138.00              | 0.0630    | 0.3574           | 0.2230              | 0.6654 | 0.6333                   | 0.2315                   |
| 410.8 | 138.07              | 0.0382    | 0.4719           | 0.0978              | 0.7723 | 0.6152                   | 0.2769                   |
| 410.9 | 138.14              | 0.0000    | 0.6107           | 0.0000              | 0.8320 | 0.5733                   | 0.3434                   |
| 410.8 | 206.86              | 0.2161    | 0.0000           | 0.9202              | 0.0000 | 0.6522                   | 0.1877                   |
| 410.9 | 206.65              | 0.2095    | 0.0285           | 0.8645              | 0.0551 | 0.6504                   | 0.1962                   |
| 410.9 | 207.00              | 0.2040    | 0.0783           | 0.7706              | 0.1405 | 0.6451                   | 0.2177                   |
| 410.9 | 206.72              | 0.1867    | 0.1812           | 0.5983              | 0.2932 | 0.6376                   | 0.2458                   |
| 410.9 | 206.65              | 0.1768    | 0.2319           | 0.5177              | 0.3597 | 0.6319                   | 0.2658                   |
| 410.9 | 206.58              | 0.1675    | 0.3061           | 0.4180              | 0.4449 | 0.6194                   | 0.2984                   |
| 410.9 | 207.14              | 0.1597    | 0.4099           | 0.3142              | 0.5248 | 0.5913                   | 0.3542                   |
| 410.8 | 207.00              | 0.1571    | 0.4480           | 0.2602              | 0.5586 | 0.5688                   | 0.3870                   |
| 410.9 | 275.79              | 0.2906    | 0.0000           | 0.9121              | 0.0000 | 0.6473                   | 0.2449                   |
| 410.9 | 275.93              | 0.2796    | 0.0738           | 0.8294              | 0.0938 | 0.6394                   | 0.2722                   |
| 410.9 | 275.93              | 0.2756    | 0.1648           | 0.6742              | 0.2109 | 0.6251                   | 0.3116                   |
| 410.9 | 276.20              | 0.2756    | 0.2398           | 0.5594              | 0.2929 | 0.6069                   | 0.3534                   |
| 410.9 | 275.51              | 0.2848    | 0.2989           | 0.4850              | 0.3378 | 0.5808                   | 0.3960                   |
| 410.8 | 275.93              | 0.2990    | 0.3306           | 0.4311              | 0.3605 | 0.5512                   | 0.4292                   |
| 410.9 | 276.07              | 0.3253    | 0.3508           | 0.3888              | 0.3686 | 0.5230                   | 0.4630                   |

the critical point at each pressure is overpredicted, as is common with calculations involving cubic equations of state. Figures 7 and 8 contain the density predictions. Once again, the densities in the liquid and near-critical regions are poorly predicted. It should be emphasized that in these ternary mixture calculations the values of the interaction parameters used were



Figure 7. Three-dimensional view of phase density data for the ternary system of nitrogen, carbon dioxide, and cyclohexane at T = 366.5 K and three pressures. The crosshatched areas represent the binary two-phase regions.

| Table V. | Binary   | Interaction | n Parameters | for | the |
|----------|----------|-------------|--------------|-----|-----|
| Peng-Rob | oinson E | quation of  | State        |     |     |

| Carbon Dioxide + (       | Cyclohexane Binary System           |
|--------------------------|-------------------------------------|
| T = 366.5  K             | $k_{\rm CO_2+C_{eH_{12}}} = 0.110$  |
| T = 410.9  K             | $k_{\rm CO_2+C_6H_{12}} = 0.103$    |
| Nitrogen + Cycl          | lohexane Binary System              |
| T = 366.5  K             | $k_{\rm N_2 + C_{eH_{12}}} = 0.109$ |
| T = 410.9  K             | $k_{\rm N_2+C_6H_{12}} = 0.076$     |
| Nitrogen + Carbon Dioxid | le + Cyclohexane Ternary System     |
| T = 366.5  K             | $k_{\rm CO_2+C_4H_{12}} = 0.110$    |
|                          | $k_{N_2+C_6H_{12}} = 0.109$         |
|                          | $k_{\rm CO_2+N_2} = 0.000$          |
| T = 410.9  K             | $k_{\rm CO_2+C_4H_{12}} = 0.103$    |
|                          | $k_{N_{9}+C_{6}H_{12}} = 0.076$     |
|                          | $k_{\rm CO_2+N_2} = 0.000$          |
|                          |                                     |

obtained from fitting the binary systems. The predictions of the ternary data involved no adjustment of the binary interaction parameters.

## Conclusions

Data are reported for the compositions and densities of the coexisting vapor and liquid phases in equilibrium for binary and ternary mixtures of nitrogen, carbon dioxide, and cyclohexane at temperatures up to 411 K and pressures to 276 bar. The compositional data for the binary systems containing cyclohexane were fit well with the Peng-Robinson equation of state with van der Waals one-fluid mixing rules, though (as is expected) the liquid density predictions were less satisfactory.



Figure 8. Three-dimensional view of phase density data for the ternary system of nitrogen, carbon dioxide, and cyclohexane at T = 410.9 K and three pressures. The crosshatched areas represent the binary two-phase regions.

Since the compositional data for constituent binary systems were reasonably well fit with the Peng–Robinson equation of state, the composition data for the ternary mixture were satisfactorily predicted by using the equation of state parameters obtained from the binary data.

### Glossary

| а               | Peng-Robinson EOS parameter for mixture     |
|-----------------|---|
| a <sub>#</sub>  | Peng-Robinson EOS parameter for component i |
| a"              | cross parameter defined by eq 4             |
| Ď               | Peng-Robinson EOS parameter for mixture     |
| b,              | Peng-Robinson EOS parameter for component i |
| k <sub>ii</sub> | binary interaction parameter                |
| n°,             | number of components in mixture             |
| NPTS            | number of experimental data points          |
| OBJ             | objective function defined by eq 5          |
| Р               | pressure                                    |
| R               | universal gas constant                      |
| Ť               | temperature                                 |
| V               | volume                                      |
| X,              | liquid mole fraction of component j         |
| ý,              | vapor mole fraction of component /          |
| Subear          | nte / eunerecrinte                          |

#### Subscripts / superscripts

| I, J | component |
|------|-----------|
|------|-----------|

- CALC calculated value
- EXP experimental value

Registry No. Carbon dioxide, 124-38-9; cyclohexane, 110-82-7; nltrogen, 7727-37-9.

# **Literature Cited**

- Shibata, S. K.; Sandler, S. I.; Kim, H. High-Pressure Vapor-Liquid Equilibria Involving Mixtures of Nitrogen, Carbon Dioxide, and *n*-Butane. J. Chem. Eng. Data 1969, 34, 291. (An erratum will follow including H. Kim as an author of this paper.).
   Krichevskii, I. R.; Sorina, G. A. Liquid-Gas Phase Equilibria in the Cy-
- (2) Krichevskii, I. R.; Sorina, G. A. Liquid-Gas Phase Equilibria in the Cyclohexane-Carbon Dioxide and Cyclohexane-Nitrous Oxide Systems. *Russ. J. Phys. Chem.* 1960, 34, 679.
- (3) Khodeeva, S. M. Tr. Naucho-Issled. Pr. I. Azotn. Prom. Org. Sin. 1971, 12, 18.
  (4) Peng, D.-Y.; Robinson, D. B. New Two-Constant Equation of State.
- (4) Peng, D.-Y.; Robinson, D. B. New Two-Constant Equation of State. Ind. Eng. Chem. Fundam. 1976, 15, 59.

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# High-Pressure Vapor-Liquid Equilibria of the Binary Mixtures Nitrogen + n-Butane and Argon + n-Butane

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High-pressure vapor-liquid equilibrium composition and density data of the binary systems nitrogen + n-butane (at 339.4 and 380.2 K) and argon + n-butane (at 340.0 and 380.1 K) are reported. The data sets were fit with the Peng-Robinson equation of state using both generalized and fluid-specific temperature-dependent parameters. The binary interaction parameters so obtained are reported.

## Introduction

This study continues our research on the vapor-liquid equilibrium of mixtures of molecules asymmetric in size and critical properties (1, 2). The data obtained in this study, in addition to being of direct interest, are of use for testing and improving equations of state and their mixing rules, especially for the simultaneous prediction of the equilibrium compositions, densities, and other thermodynamic properties of mixtures.

#### Experiment

A dynamic high-pressure vapor-liquid equilibrium apparatus (maximum pressure 5000 psi and maximum temperature 300 °F), which allows the simultaneous measurement of the compositions and densities of the coexisting phases, was used to obtain the data reported below. Shibata et al. (1) give a detailed description of the apparatus and its operation.

Grade 5 nitrogen, argon with a purity of 99.998%, and instrument grade *n*-butane, supplied by Matheson were used for the measurements. As described earlier (1), temperatures are measured with an error of less than 0.05 K and pressures with an error of 0.1 psi in the range below 800 psi and 2 psi above 800 psi. The error in the measurement of the phase compositions with a calibrated gas chromatograph is smaller than 0.005 mole fraction. Densitles were measured with calibrated Mettler/Paar vibrating tube densimeters with an error of less than 0.0001 g/cm<sup>3</sup>.

## **Results and Discussion**

Tables I and II give the unsmoothed data for the equilibrium compositions and densities for the nitrogen + n-butane system

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Table I. Experimental Data for the Nitrogen + n-Butane System at 339.4 K

| <i>Т</i> , К    | P, bar | x <sub>N</sub> | УN    | $^{ ho_{ m L},}_{ m g/cm^3}$ | $p_{V}, g/cm^3$ |  |
|-----------------|--------|----------------|-------|------------------------------|-----------------|--|
| 339.37          | 12.41  | 0.023          | 0.342 | 0.5242                       | 0.0263          |  |
| 339.18          | 18.82  | 0.024          | 0.524 | 0.5230                       | 0.0333          |  |
| 339.26          | 26.17  | 0.038          | 0.632 | 0.5226                       | 0.0413          |  |
| 339.43          | 34.35  | 0.051          | 0.700 | 0.5212                       | 0.0514          |  |
| 339.36          | 41.66  | 0.068          | 0.738 | 0.5203                       | 0.0596          |  |
| 33 <b>9.4</b> 1 | 56.16  | 0.092          | 0.781 | 0.5190                       | 0.0766          |  |
| 339.41          | 68.26  | 0.117          | 0.800 | 0.5175                       | 0.0916          |  |
| 399.33          | 89.18  | 0.165          | 0.822 | 0.5144                       | 0.1196          |  |
| 339.39          | 103.42 | 0.180          | 0.826 | 0.5120                       | 0.1356          |  |
| 339.57          | 120.52 | 0.211          | 0.824 | 0.5095                       | 0.1578          |  |
| 339.35          | 135.96 | 0.249          | 0.824 | 0.5042                       | 0.1788          |  |
| 339.37          | 152.17 | 0.282          | 0.815 | 0.4869                       | 0.2001          |  |
| 339.50          | 168.85 | 0.315          | 0.801 | 0.4810                       | 0.2249          |  |
| 339.48          | 182.64 | 0.352          | 0.792 | 0.4746                       | 0.2479          |  |
| 339.37          | 193.88 | 0.381          | 0.778 | 0.4685                       | 0.2649          |  |
| 339.35          | 199.95 | 0.400          | 0.761 | 0.4640                       | 0.2770          |  |
| 339.35          | 206.29 | 0.424          | 0.751 | 0.4563                       | 0.2888          |  |
| 339.15          | 215.18 | 0.459          | 0.726 | 0.4467                       | 0.3098          |  |
| 339.35          | 221.05 | 0.505          | 0.688 | 0.4201                       | 0.3360          |  |
|                 |        |                |       |                              |                 |  |

Table II. Experimental Data for the Nitrogen + n-Butane System at 380.2 K

| <i>Т</i> , К | P, bar | x <sub>N</sub> | УN    | $^{ ho_{ m L}}_{ m g/cm^3}$ | $p_{\rm v}, g/{\rm cm}^3$ |
|--------------|--------|----------------|-------|-----------------------------|---------------------------|
| 380.15       | 17.58  | 0.000          | 0.000 | 0.4518                      | 0.0483                    |
| 380.02       | 24.27  | 0.020          | 0.190 | 0.4501                      | 0.0566                    |
| 380.20       | 31.92  | 0.037          | 0.319 | 0.4478                      | 0.0649                    |
| 380.26       | 39.44  | 0.051          | 0.400 | 0.4458                      | 0.0748                    |
| 380.07       | 51.64  | 0.077          | 0.483 | 0.4409                      | 0.0904                    |
| 380.09       | 65.50  | 0.109          | 0.540 | 0.4348                      | 0.1105                    |
| 380.21       | 82.74  | 0.153          | 0.573 | 0.4254                      | 0.1349                    |
| 380.20       | 103.42 | 0.211          | 0.586 | 0.4097                      | 0.1700                    |
| 380.20       | 124.04 | 0.287          | 0.563 | 0.3833                      | 0.2153                    |
| 380.30       | 130.66 | 0.317          | 0.544 | 0.3634                      | 0.2369                    |
| 380.25       | 134.45 | 0.349          | 0.514 | 0.3489                      | 0.2560                    |
| 380.35       | 135.76 | 0.373          | 0.500 | 0.3370                      | 0.2707                    |

at 339.4 and 380.0 K, respectively; these same data are plotted in Figures 1 and 2. The data for the argon + n-butane system at the same temperatures are shown in Tables III and IV and in Figures 3 and 4. The data were fit with the Peng–Robinson equation of state (PR-EOS) (3) with both generalized parameters and the fluid-specific temperature-dependent parameters of Xu and Sandler (4). The PR-EOS can be written as

$$P = \frac{RT}{v - b} - \frac{a}{v(v + b) + b(v - b)}$$
(1)

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